



Development of a Prediction Model for High pCO₂ Corrosion of Mild Steel

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ABSTRACT

Most of the corrosion prediction models used for design of oil and gas lines carrying high pCO $_2$ are valid up to 1 ~ 2 MPa of pCO $_2$ and are very conservative at higher pCO $_2$ because they do not account for the effect of high pCO $_2$ on the water chemistry and the corrosion mechanism. The present work was focused on developing a predictive tool for near-critical and supercritical CO $_2$ corrosion of mild steel. It incorporates changes in the water chemistry module due to update solubility and dissociation equations, changes in the electrochemical module due to the presence of a thick and porous corrosion product layer, and consideration of an adsorption mechanism for H_2CO_3 at the steel surface. The comparison between experimental results and model predictions showed a good agreement under various pressure and temperature ranges.

Key words: Supercritical CO₂, CO₂ corrosion, carbon steel, corrosion model

INTRODUCTION

Internal corrosion of carbon steel pipeline in high partial pressure CO₂ (pCO₂) environments have gained more interest recently relating to carbon capture and storage (CCS), enhanced oil recovery (EOR), and deep water oil and gas production applications.1⁻⁵ Although there are extensive research data available on high pCO₂ corrosion, minimal information has been reported in the literature that could aid in

establishing a corrosion model for carbon steel in such conditions.6-8 Furthermore, the published literature on supercritical CO2 primarily addresses topics related to sequestration and enhanced oil recovery (EOR) that usually involve "dry" gases where water is only present at the ppm level.

The impact of aqueous CO₂ corrosion on carbon steel has been studied extensively at pressures relevant for oil and gas transport (up to 2 MPa CO₂). Therefore, most of the predictive models used for design of oil and gas lines carrying high pCO₂ are valid up to 1 ~ 2 MPa of pCO₂ and are very conservative at higher pCO₂.9⁻¹²

It has been reported that aqueous corrosion mechanisms in high pCO₂ are similar to those in low pCO₂ conditions including characteristics of corrosion product layer and the response of corrosion rate with temperature. 13 This indicates that the existing CO₂ corrosion model could be used to predict the corrosion rate at high pCO₂ conditions with some modifications in chemical, electrochemical or transport processes. For example, since CO₂ changes from gaseous to liquid or supercritical with increasing pressure, it will lead to different interaction with water, i.e. CO₂ solubility in water will not follow Henry's law in liquid or supercritical CO₂ conditions, which results in changing water chemistry.¹⁴

Thus, the objective of the present study was to develop a predictive model for high pCO₂ corrosion of mild steel considering with changes in chemical and electrochemical reactions.

MODEL DESCRIPTION

The mechanistic model developed by Nesic et al., in early 2000 covers most of the key processes present in uniform CO2 corrosion of carbon steel: electrochemical reactions at the steel surface, chemical reactions and transport of species between the steel surface and the bulk solution, and formation/growth of iron carbonate (FeCO₃) layer. The physical, mathematical, and numerical aspects of the model are explained in detail in the previous papers. 15-18 In the present study, this model was used as a base platform and the key aspects of the model are briefly described below:

Water Chemistry Model

Understanding water chemistry is an important precondition for predicting CO₂ corrosion of carbon steel. Various chemical reactions take place in the water phase due to the presence of CO₂. For a CO₂ aqueous system, the following reactions are taken into consideration at all times:

$$CO_{2(g)} \stackrel{\text{Ksol}}{\longleftrightarrow} CO_{2(aq)} \text{ (Dissolution of CO}_2) \tag{1}$$

$$CO_{2(aq)} + H_2O \stackrel{\text{Khyd}}{\longleftrightarrow} H_2CO_3 \text{ (Hydration of aqueous CO}_2) \tag{2}$$

$$CO_{2(aq)} + H_2O \xrightarrow{Khyd} H_2CO_3$$
 (Hydration of aqueous CO_2) (2)

$$H_2CO_3 \stackrel{\text{Kca}}{\longleftrightarrow} H^+ + HCO_3^-$$
 (Dissociation of carbonic acid) (3)
 $HCO_3 \stackrel{\text{Kbi}}{\longleftrightarrow} H^+ + CO_3^{2-}$ (Dissociation of bicarbonate ion) (4)
 $H_2O \stackrel{\text{Kw}}{\longleftrightarrow} H^+ + OH^-$ (Dissociation of water) (5)

$$HCO_3^- \stackrel{Kbi}{\longleftrightarrow} H^+ + CO_3^{2-}$$
 (Dissociation of bicarbonate ion) (4)

$$H_2O \xrightarrow{KW} H^+ + OH^-$$
 (Dissociation of water) (5)

The reactions shown above can be described by equilibria reactions as follows based on the assumption of infinite dilution:

$$K_{sol} = \frac{C_{CO_{2(aq)}}}{P_{CO_{2(g)}}}$$

$$K_{hyd} = \frac{C_{H_2CO_3}}{C_{CO_2}C_{H_2O}}$$

$$K_{ca} = \frac{C_{H^+}C_{HCO_3^-}}{C_{H_2CO_3}}$$
(8)

$$K_{hyd} = \frac{C_{H_2CO_3}}{C_{CO_2} C_{H_2O}}$$
 (7)

$$K_{ca} = \frac{C_{H^+} C_{HCO_3^-}}{C_{H_2CO_3}}$$
 (8)

$$K_{bi} = \frac{C_{H^{+}} C_{CO_{3}^{2}}}{C_{HCO_{3}^{-}}}$$

$$K_{W} = \frac{C_{H^{+}} C_{OH^{-}}}{C_{H_{2}O}}$$
(9)

$$K_{W} = \frac{C_{H^{+}} C_{OH^{-}}}{C_{H_{2}O}}$$
 (10)

 $\text{where } C_{CO_2},\,C_{H_2CO_3},\,C_{HCO_3^-},\,C_{CO_3^{2-}},\,C_{H^+},\,\text{and }C_{OH^-}\text{ are the concentrations (mol/L) of }CO_2,\,\text{carbonic acid},\,C_{CO_3^{2-}},\,C_{H^+},\,\text{and }C_{OH^-},\,C_{OH^$ bicarbonate ion, carbonate ion, hydrogen ion, and hydroxide ion, respectively.

The equilibrium constants, K, are a function of the temperature and are available in the open literature. Since the solution cannot have a net charge, an electroneutrality relation is required. Mathematically, it is expressed:

$$C_{H^{+}} = C_{HCO_{3}^{-}} + 2 \times C_{CO_{3}^{2-}} + C_{OH^{-}}$$
(11)

Electrochemical Model

As the CO₂ corrosion process is electrochemical in nature, the corrosion rate can be explicitly determined by calculating the rate of the electrochemical reactions occurring simultaneously at the steel surface:

Anodic (oxidation) reaction:

$$Fe \rightarrow Fe^{2+} + 2e- \tag{12}$$

Cathodic (reduction) reactions:

$$H^+ + e^- \rightarrow \frac{1}{2}H_2$$
 (13)

$$H_2CO_3 + e^- \rightarrow \frac{1}{2}H_2 + HCO_3$$
 (14)

The electrochemical reaction rate can be expressed as a current density, i (expressed in $A m^{-2}$), which is a function of the potential at the metal surface, *E* (expressed in *V*):

$$i=\pm i_0 \times 10^{\pm \frac{E-E_{rev}}{b}} \times \prod_{s=1}^{n_s} (1-\theta_s)$$
 (15)

This equation is unique for each of the electrochemical reactions involved in a corrosion process such as iron oxidation, hydrogen reduction and carbonic acid reduction. The "+" sign applies for anodic reactions while the "-" sign applies for cathodic reactions. θ_s is the fraction of the steel surface where a given electrochemical reaction does not occur because the surface is covered by a species s which could be an adsorbed inhibitor or a protective film. The product sign \(\pi\) accounts for a compounding (additive) effect by more than one surface species. For each electrochemical reaction, Equation (1) is different because of the parameters defining it: i_0 - the exchange current density in $A m^{-2}$, E_{rev} - the reversible potential in V, and b - the Tafel slope in V. These parameters have to be determined experimentally and are functions of temperature and in some cases species concentrations. The unknown potential at the metal surface E in Equation (15), is also called the corrosion potential or open circuit potential, which can be found from the charge balance equation at the metal surface:

$$\sum_{a=1}^{n_a} i_a = \sum_{c=1}^{n_c} i_c \tag{16}$$

where n_a and n_c are the total number of anodic and cathodic reactions respectively.

FeCO₃ Layer Formation and Growth Model

Solid FeCO₃ forms when the concentrations of Fe²⁺ and CO₃²⁻ exceed the solubility limit according to the following reaction:

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$$\operatorname{Fe}^{2+}_{(aq)} + \operatorname{CO}_{3(aq)}^{2-} \leftrightarrow \operatorname{FeCO}_{3(s)} \tag{17}$$

When FeCO₃ precipitates on the steel surface, it can slow down the corrosion process not only by presenting a diffusion barrier for the species involved in the corrosion process but also by blocking a portion of the steel surface and preventing the underlying steel from further corrosion.

The governing equation for FeCO₃ layer growth based on mass conservation of FeCO₃ in the solution is shown in equation (18).

$$\frac{\partial \varepsilon}{\partial t} = \frac{M_{\text{FeCO}_3}}{\rho_{\text{FeCO}_3}} \frac{A}{V} R_{\text{FeCO}_3} - CR \frac{\partial \varepsilon}{\partial x}$$
(18)

where ε is porosity, t is time, M_{FeCO_3} is molar mass of FeCO₃, ρ_{FeCO_3} is density of FeCO₃, $\frac{A}{V}$ is area-volume ratio, R_{FeCO_3} is precipitation rate of FeCO₃, CR is corrosion rate, and x is distance. In this equation, FeCO₃ layer growth is characterized by the change in porosity (ε), which changes between 0 and 1. A value of 1 indicates that no FeCO₃ layer forms while a value of 0 represents that the surface is completely filled with FeCO₃. This equation suggests that the growth of FeCO₃ layer is attributed to two factors: FeCO₃ precipitation and undermining steel corrosion. Depending on the relative values of these two terms, FeCO₃ layer can be either protective or non-protective.

RESULTS AND DISCUSSION

Modification in Water Chemistry Model

In low pCO₂ system, the concentration of dissolved CO₂ in water is directly proportional to its partial pressure (Equation 1). The solubility constant is calculated and derived using Henry's constant (K_{sol}) as the concentration of dissolved CO₂ is relatively small. In high pCO₂ systems, however, the relationship between concentration and pressure is not linear and Henry's law cannot be used directly. Instead, the non-ideality of the CO₂ phase must be taken into account. In the present study, two different CO₂ solubility models were selected from open literature for high pCO₂ conditions¹⁹⁻²¹ and compared with the case with Henry's law. Figure 1 shows the comparison of mole fraction of CO₂ in water as a function of pCO₂ calculated from different solubility models at 25°C and 60°C. It shows that the amount of dissolved CO₂ increased with increasing pCO₂. It can be also seen that as pCO₂ increases, the solubility of CO₂ in water deviates further from Henry's Law; that is, the domain of validity of Henry's Law is at best 2 MPa at 25°C, and only 0.8 MPa at 60°C.²² In addition, there is no significant difference in CO₂ content between the high pCO₂ solubility models.

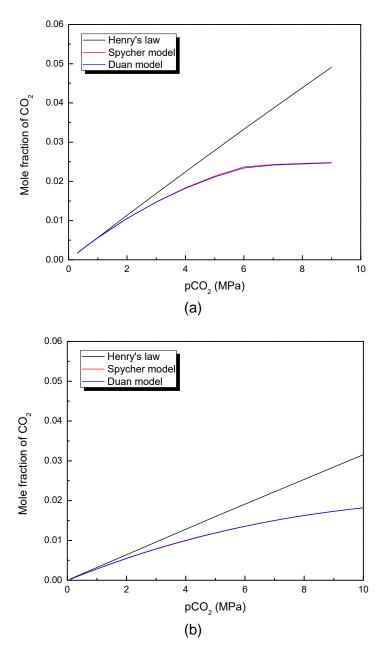


Figure 1: Comparison of the calculated molar fraction of dissolved CO₂ in water based on Henry's law and high pCO₂ solubility models as a function of pCO₂: (a) 25°C, (b) 60°C.

Other equilibrium constants were also compared between low pCO₂ and high pCO₂ models. For example, the equilibrium constant for carbonic acid dissociation (K_{ca}) is calculated in the low pCO₂ model as:¹⁵

$$K_{ca} = 387.6 \times 10^{-(6.41 - 1.594 \times 10^{-3} T_f + 8.52 \times 10^{-6} T_f^2 - 3.07 \times 10^{-5} p - 0.4772 \times I^{\frac{1}{2}} + 0.118 \times I)}$$
(19)

where T_f is the temperature in degrees Fahrenheit, p is the pressure in psi and I is the ionic strength in molar. For the high pCO₂ model, K_{ca} was taken from open literature that can cover the temperature range of 0°C to 100°C and the pressure range of 0.1 to 300 MPa:^{23,24}

$$\ln K_{ca} = 233.5159304 - 11974.38348T^{-1} - 36.50633536 \ln T + (-45.08004597T^{-1} + 2131.318848T^{-2} + 6.714256299T^{-1} \ln T)(P - P_S) + (0.008393915212T^{-1} - 0.4015441404T^{-2} - 0.00124018735T^{-1})(P - P_S)^2$$
 (20)

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where P_s is the saturation pressure of water, P is the CO_2 pressure in bar, and T is the temperature in Kelvin. Figure 2 compares the pK_{ca} values as a function of pCO_2 calculated by Equation 16 and Equation 17 at 25°C and 60°C. Although the pK_{ca} of high pCO_2 model was slightly higher than that of low pCO_2 model, it will not cause a significant difference in the calculation of species concentrations. The same trend was observed for the comparison of other equilibrium constants between low pCO_2 model and high pCO_2 model.

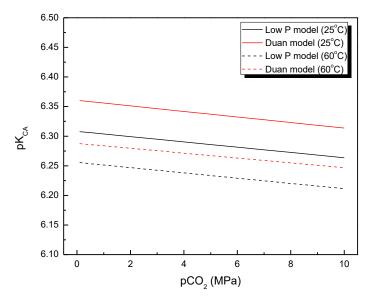
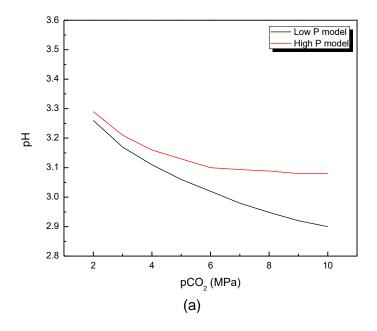


Figure 2: Comparison of the pK_{ca} calculated by low pCO_2 model and high pCO_2 model as a function of pCO_2 at 25°C and 60°C.

Figure 3 shows the pH values as a function of pCO₂ calculated by low pCO₂ model and high pCO₂ model at 25°C and 60°C. The pH values decreased with increasing pCO₂ due to the increase of the dissolved CO₂ amount (Figure 1). However, a significant effect of non-ideal behavior of CO₂ at high pressures on the pH can be seen due to the deviation from the solubility calculations based on Henry's law and the high pCO₂ solubility model. This result suggests that utilizing the low pCO₂ water chemistry model could overestimate the corrosion rate in high pCO₂ conditions due to the inaccurate prediction of pH.



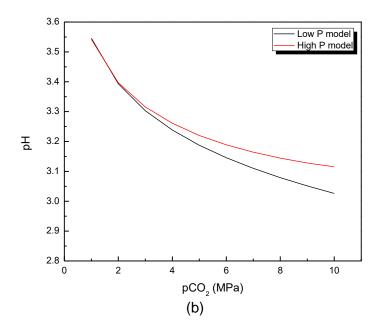


Figure 3: Comparison of the calculated solution pH based on low pCO₂ model and high pCO₂ model as a function of pCO₂: (a) 25°C, (b) 60°C.

Modification in Electrochemical Model

The modified water chemistry model was implemented and the corrosion rate was predicted in conjunction with the original electrochemical model. However, the corrosion rates were still overpredicted as compared to experimental data by a factor of 2 to 4.

If the species concentrations are predicted correctly with the high pCO₂ water chemistry model, then the over prediction of corrosion rates may be a result of not considering the limited ability for the corrosive species to adsorb on the steel surface in order to be reduced. In other words, it can be assumed that all the increased concentrations of species, such as H⁺ and H₂CO₃ due to the increase in pCO₂ can not adsorb to the metal surface due to the reaction site limitations. Therefore, the cathodic reduction reactions become limited by adsorption kinetics resulting in plateau for the corrosion rate at high pCO₂ conditions. This phenomenon was implemented using a Langmuir adsorption isotherm:

$$\theta = 1 - \frac{K.pCO_2}{1 + K.pCO_2} \tag{21}$$

where θ is the fractional surface coverage for species at the steel surface, and K is the adsorption equilibrium constant. The value of θ determines availability of the reducible species at the surface. Figure 4 shows the fractional surface coverage coefficient as a function of pCO₂.

Since H_2CO_3 is by far the main cathodic species in the corrosion reaction at high pCO_2 conditions (as compared to H^+), the implementation of the adsorption coefficient Θ has been applied to the calculation of the current density of H_2CO_3 reduction reaction. This will reduce the influence of H_2CO_3 on the corrosion behavior and consequently dampen the corrosion rates at high pCO_2 conditions.

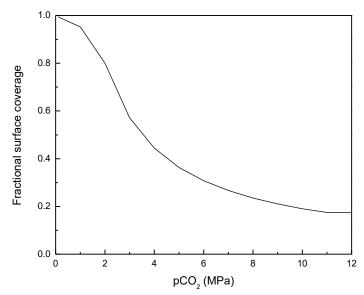


Figure 4: Fractional surface coverage coefficient as a function of pCO₂.

Modification in FeCO₃ Layer Formation and Growth Model

Solving equation (15) accounts several numerical issues. For example, the first term on the right hand side (RHS) of equation (15) is a hyperbolic equation with stiff non-linear source term. Furthermore, the second term on the RHS of equation (15) poses a convective-like effect in the equation. A convective term contributes to numerical instability in solving a partial differential equation, which includes incorrect front propagation and severe limit on time step. The numerical instability is more pronounced at high pCO₂ conditions. Thus in the present study, to minimize numerical instability, the hyperbolic precipitation rate equation was solved implicitly using exact analytical solution and front tracking scheme ($\varepsilon_{i,j}^{n+1} = \varepsilon_{i,j-1}^n$) was implemented for the convective component.

Equation (15) is solved in the 1D domain as shown in Figure 5. At the FeCO₃ layer/metal surface interface, the porosity is considered to be 1, as the corrosion process continuously creates voids underneath the FeCO₃ layer. At the other boundary (between the diffusion boundary layer and the bulk solution), it is assumed that no FeCO₃ can grow onto the boundary and out of the domain; therefore, porosity of FeCO₃ maintains at 1.

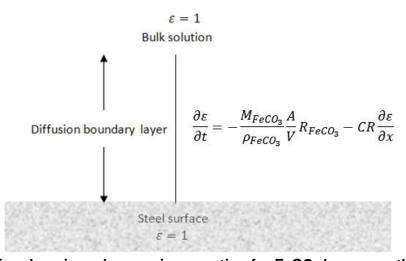


Figure 5: Computation domain and governing equation for FeCO₃ layer growth simulation.

Parametric Study

Figure 6 shows the effect of pCO₂ on corrosion rate from model prediction for different pH values at 80° C. It is seen that the corrosion rate increases with increasing pCO₂ for both pH values. Figure 7 shows the effect of temperature on corrosion rate at 12 MPa of pCO₂. The corrosion rate increases with the increase in temperature due to the higher reaction rate at higher temperature. It is also observed that the corrosion rate changed greatly from 50° C to 80° C. Figure 8 represents the effect of pH on corrosion rate at 12 MPa of pCO₂ and 80° C. The corrosion rate slightly decreases from pH 3 to 5 and then it decreases to very low corrosion rate at pH 6 due to the formation of protective FeCO₃. Figure 9 shows the effect of flow velocity on corrosion rate for different temperatures at 12 MPa of pCO₂ and pH 3. It is observed that the increase in flow velocity accelerates the corrosion reaction at higher temperature (80° C).

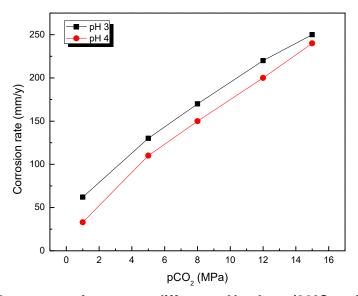


Figure 6: Effect of pCO₂ on corrosion rate at different pH values (80°C and 1 m/s flow velocity).

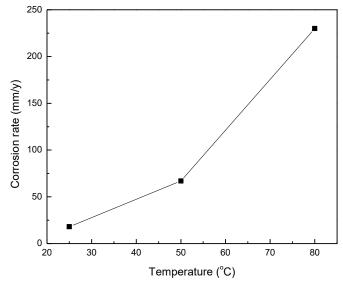


Figure 7: Effect of temperature on corrosion rate at pH 3 (12 MPa pCO₂ and 1 m/s flow velocity).

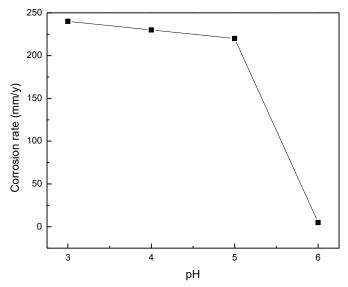


Figure 8: Effect of pH on corrosion rate at 80°C (12 MPa pCO₂ and 1 m/s flow velocity).

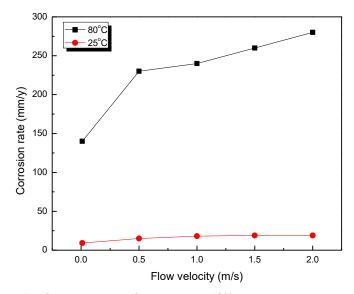
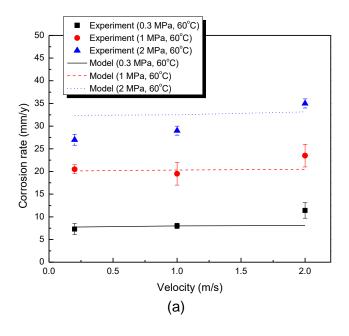
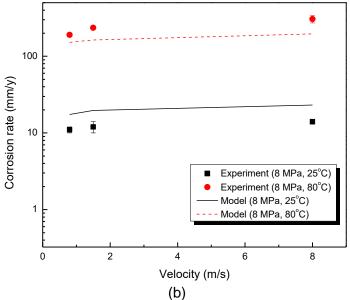


Figure 9: Effect of flow velocity on corrosion rate at different temperatures (12 MPa pCO₂ and pH 3).

Model Validation

The comparison between experimental data (obtained from autoclave and high pressure flow loop experiments)²⁵⁻²⁷ and model prediction is shown in Figure 10 under different combinations of pressure and temperature. The predicted corrosion rates show a good agreement with experimental data. Many similar comparisons were made for other conditions covered in this study, with similar results.





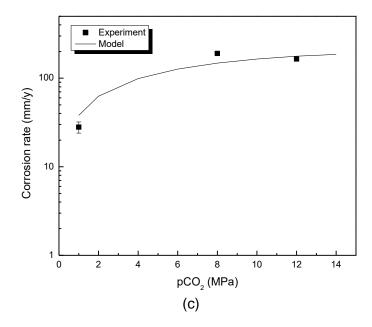


Figure 10: Comparison of corrosion rates between experiments and predictions in CO₂ environments at different conditions: (a) 0.3 ~ 2 MPa CO₂, 60°C, pH 5, (b) 8 MPa CO₂, 25°C ~ 80°C, pH 3.1 ~ 3.2, (c) 1 MPa ~ 14 MPa CO₂, 80°C, pH 3.1 ~ 3.4.

CONCLUSIONS

A predictive model was developed for corrosion of carbon steel in high pCO₂ conditions by modifying the existing CO₂ corrosion model for low pCO₂. The following conclusions are drawn:

- Water chemistry model was changed by considering non-ideality of the CO₂ phase.
- Electrochemical model was updated by including the Langmuir adsorption isotherm for H₂CO₃.
- FeCO₃ formation and growth model was improved by implementing front tracking scheme and exact analytical solution in order to avoid numerical instability.
- Corrosion rates predicted by the updated model showed a good agreement with experimental data under various high pCO₂ conditions.

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